

**AUSTRALIAN DEFENCE FORCE ACADEMY  
 SCHOOL OF  
 AEROSPACE AND MECHANICAL ENGINEERING**

**Course: AMEC 3508 Mechanics of Solids 2B  
 AMEC 3706 Aircraft Structures 1B**

**Assignment #1 (30%)**

**Due date: Monday, September 17, 2001, 23:59**

The truss in Fig.1 is made of hollow tubes with Young's modulus **E**.  
 The tubes have inner radius **R<sub>in</sub>** and outer radius **R<sub>out</sub>**

The elemental stiffness matrix for 2D truss is:

$$[ke] = \frac{A \cdot E}{L} \begin{bmatrix} \cos^2 \alpha & \cos \alpha \sin \alpha & -\cos^2 \alpha & -\cos \alpha \sin \alpha \\ \cos \alpha \sin \alpha & \sin^2 \alpha & -\cos \alpha \sin \alpha & -\sin^2 \alpha \\ -\cos^2 \alpha & -\cos \alpha \sin \alpha & \cos^2 \alpha & \cos \alpha \sin \alpha \\ -\cos \alpha \sin \alpha & -\sin^2 \alpha & \cos \alpha \sin \alpha & \sin^2 \alpha \end{bmatrix}$$

**A**= cross section area

**L**= element length where  $L = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$  and  $\cos \alpha = \frac{x_2 - x_1}{L}$ ,  $\sin \alpha = \frac{y_2 - y_1}{L}$

Write a MATLAB function **A1\_yourStudentID.m** with the following declaration:

**%FEM Assignment #1, Parametric Truss Analysis**

**function [RES]= A1\_yourStudentID (E,Rin,Rout,h1,h2,L4,L6,L10,F,ALPHA)**

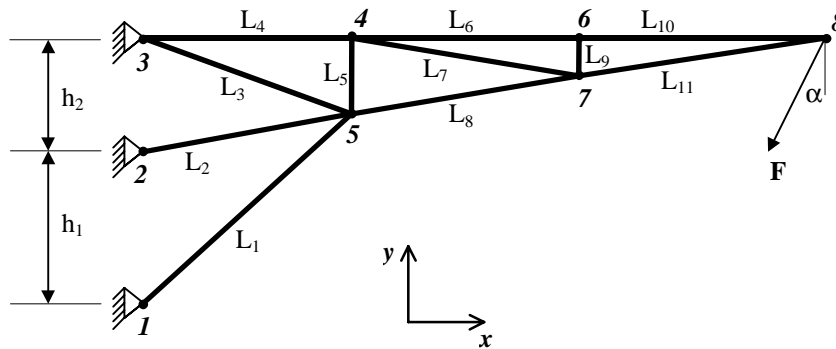
**Required numerical results (162 points in total):**

1. (10pts) Obtain all the elemental stiffness matrices in a 4 by 4 by 11 array in **RES.KE**
2. (30pts) Obtain all the blown-up elemental stiffness matrices in a 16 by 16 by 11 array in **RES.KEB**
3. (10pts) Obtain the global stiffness matrix in a an array in **RES.KGLB**
4. Introduce the boundary conditions and obtain the reduced:
  - a) (10pts) Global stiffness matrix in **RES.KGBC**
  - b) (10pts) Global displacement matrix in **RES.DBC**
  - c) (10pts) Global force matrix in **RES.FBC**
5. (10pts) Use the provided "Gaussian Elimination" function to obtain all displacements in **RES.DISPS**
6. (12pts) Obtain all the reaction forces in **RES.FORCES**
7. (30pts) Obtain all axial forces in **RES.AXLF**
8. (10pts) Obtain all axial stresses in **RES.AXSTRS**
9. (5pts) Obtain the maximum tensile stress **RES.MXTSTRS** and its element number **RES.MXTLOC**

10. (5pts) Obtain the minimum tensile stress **RES.MNTSTRS** and its element number **RES.MNTLOC**
11. (5pts) Obtain the maximum compressive stress **RES.MXCSTRS** and its element number **RES.MXCLOC**
12. (5pts) Obtain the minimum compressive stress **RES.MNCSTRS** and its element number **RES.MNCLOC**

Use the following formulae in numbering the forces and displacements:

$$F_x^n = F_{2n-1} \quad F_y^n = F_{2n} \quad \text{and} \quad x_n = \delta_{2n-1} \quad y_n = \delta_{2n} \quad \text{where } n \text{ is the node number.}$$



**Figure 1.**

**Hints:**

- $L_4$ ,  $L_6$  and  $L_{10}$  are horizontal
- $L_2$ ,  $L_8$  and  $L_{11}$  make up a straight line from node 2 to node 8
- Use geometric properties to calculate the rest of the dimensions and the coordinates of each node.

**IMPORTANT:**

Submission and assessment of this assignment will be done **electronically**. E-mail your MATLAB function as an attachment to [m.tahtali@adfa.edu.au](mailto:m.tahtali@adfa.edu.au), with **exactly** [FEM2001-A1] in the subject field. Do not submit a function that:

- does not terminate properly
- does not return any values
- crashes
- or hangs